

Calculus

Story Problem Celebration #2

29 a) \$700 per item

b) \$500 per item

c) \$300 per item

d) $\lim_{h \rightarrow 0} \frac{P(4+h) - P(4)}{h}$

$$\lim_{h \rightarrow 0} \frac{2(16+8h+h^2) - 5(4+h) + 6 - 18}{h}$$

$$\lim_{h \rightarrow 0} \frac{32 + 16h + 2h^2 - 20 - 5h - 12}{h}$$

$$\lim_{h \rightarrow 0} \frac{11h + 2h^2}{h} = \lim_{h \rightarrow 0} 11 + 2h = \boxed{\$1100 \text{ per item}}$$

30 a) \$5998

b) \$6000

c) \$5998

d) a & c are =

32 $\lim_{S \rightarrow \infty} P(S) = \boxed{63}$; No matter how many days of training the production maxs out at 63 items/day.

33 a) $\frac{P(4) - P(1)}{4 - 1} = \frac{20 - 2}{3} = \frac{18}{3} = \boxed{6\% \text{ per day}}$

b) $\lim_{h \rightarrow 0} \frac{P(3+h) - P(3)}{h} = \lim_{h \rightarrow 0} \frac{(3+h)^2 + (3+h) - 12}{h} = \lim_{h \rightarrow 0} \frac{9 + 6h + h^2 + 3 + h - 12}{h}$

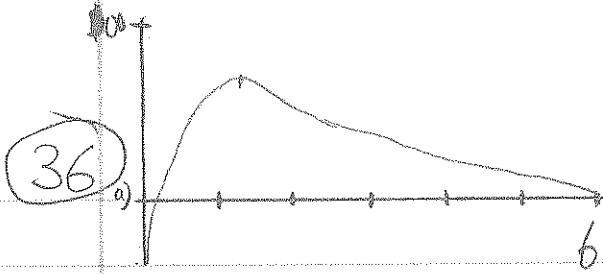
$$= \lim_{h \rightarrow 0} \frac{7h + h^2}{h} = \lim_{h \rightarrow 0} 7 + h = \boxed{7\% \text{ per day}}$$

35 a) $\frac{L(28) - L(22)}{28 - 22} = \frac{7.176 - 5.448}{6} = \boxed{.288 \text{ mm/week}}$

b) $\lim_{h \rightarrow 0} \frac{L(22+h) - L(22)}{h} = \frac{-.01(22+h)^2 + .788(22+h) - 7.048 - 5.448}{h}$

$$\lim_{h \rightarrow 0} \frac{-4.84 - .44h - .01h^2 + 17.336 + .788h - 12.496}{h} = \lim_{h \rightarrow 0} \frac{.348h - .01h^2}{h}$$

$$= \lim_{h \rightarrow 0} .348 - .01h = \boxed{.348 \text{ mm/week}}$$



$$b) \frac{F(1) - F(0)}{1 - 0} = \frac{71.226 - 10.28}{1}$$

$$= 81.506 \frac{\text{kJ}}{\text{hr}} \text{ per hour}$$

$$c) 18.81 \frac{\text{kJ}}{\text{hr}} \text{ per hour}$$

$$d) t = 1.3 \text{ hours}$$

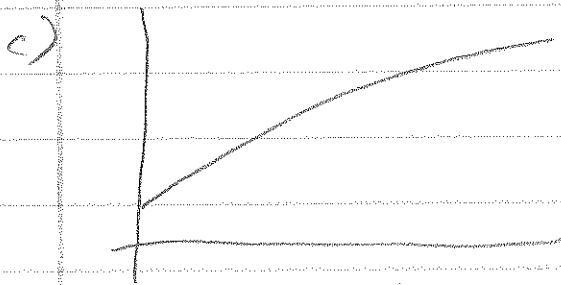
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$$a) \frac{M(115) - M(105)}{115 - 105} = \frac{48.775 - 47.975}{10} = 0.08 \text{ kg/100g}$$

$$b) \lim_{h \rightarrow 0} \frac{M(105+h) - M(105)}{h} = \lim_{h \rightarrow 0} \frac{27.5 + .3(105+h) - .001(105+h)^2 - 47.975}{h}$$

$$= \lim_{h \rightarrow 0} \frac{27.5 + 31.5 + .3h - 11.025 - 2.1h - .001h^2 - 47.975}{h} = \frac{47.975 - .001h^2}{h}$$

$$\lim_{h \rightarrow 0} \frac{-1.8h - .001h^2}{h} = \lim_{h \rightarrow 0} -1.8 - .001h = -1.8$$



d) NO, mass should keep increasing not flatten out as graph does

41) a) $\frac{10-0}{2-0} = 5 \frac{\text{ft}}{\text{sec}}$ b) $\frac{14-10}{4-2} = \frac{4}{2} = 2 \frac{\text{ft}}{\text{sec}}$

c) $\frac{20-14}{6-4} = \frac{6}{2} = 3 \frac{\text{ft}}{\text{sec}}$ d) $\frac{30-20}{8-6} = \frac{10}{2} = 5 \frac{\text{ft}}{\text{sec}}$

e) i) $\frac{20-10}{6-2} = \frac{10}{4} = 2.5 \frac{\text{ft}}{\text{sec}}$ f) i) $\frac{30-14}{8-4} = \frac{16}{4} = 4 \frac{\text{ft}}{\text{sec}}$

ii) $\frac{3+2}{2} = 2.5 \text{ ft/sec}$

ii) $\frac{5+3}{2} = 4 \frac{\text{ft}}{\text{sec}}$

g) No it will not always be the same.