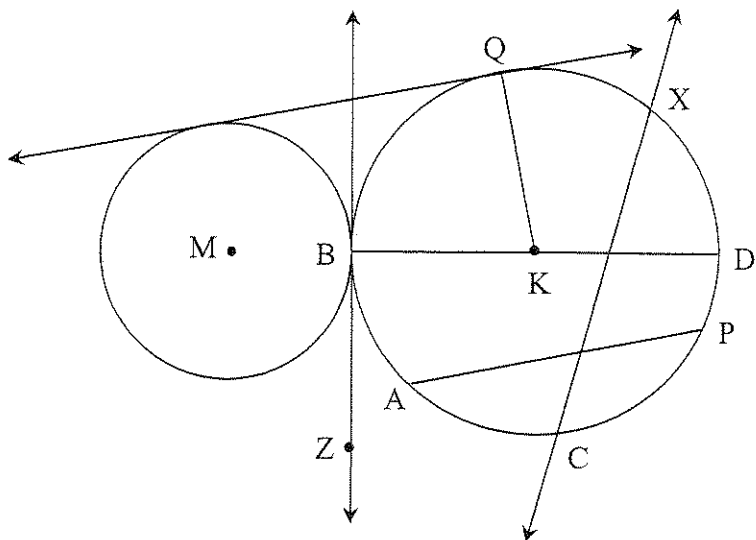


Properties of Circles

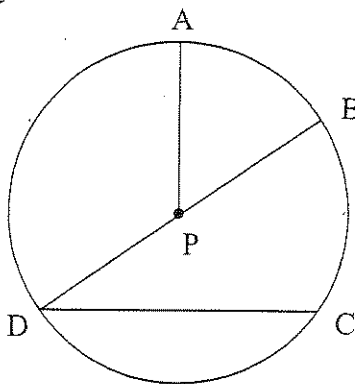
1. Identify the line or segment in  $\odot K$  or  $\odot M$  that is best described by the term.



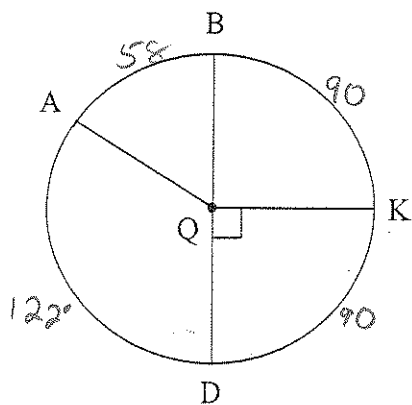
- a. chord  $\overline{AP}, \overline{YZ}, \overline{BD}$
- b. secant  $\overleftrightarrow{XC}$
- c. diameter  $\overline{BD}$
- d. radius  $\overline{KQ}, \overline{KD}, \overline{KB}$
- e. common internal tangent  $\overline{BE}$
- f. common external tangent  $\overline{ZQ}$
- g. all points of tangency  $B, Q$
- h. 2 perpendicular lines  $\overline{BE} \perp \overline{BD}$   
 $\overline{KQ} \perp \overline{BE}$

2. Identify an angle or arc in  $\odot P$  that is described by the term.

- a. minor arc  $\widehat{AB}, \widehat{AD}, \widehat{DC}, \widehat{BC}, \widehat{AC}$
- b. inscribed angle  $\angle D$
- c. central angle  $\angle APB, \angle APD$
- d. major arc  $\widehat{ABD}, \widehat{BCA}, \widehat{BAC}$
- e. semicircle  $\widehat{BD}$



3. Find the measures in  $\odot Q$  given that  $m\widehat{AB} = 58^\circ$ .



$$m\angle AQB = 58^\circ$$

$$m\widehat{AD} = 122^\circ$$

$$m\widehat{AK} = 148^\circ$$

$$m\widehat{ABD} = 238^\circ$$

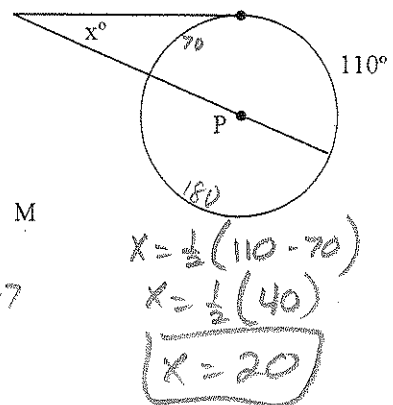
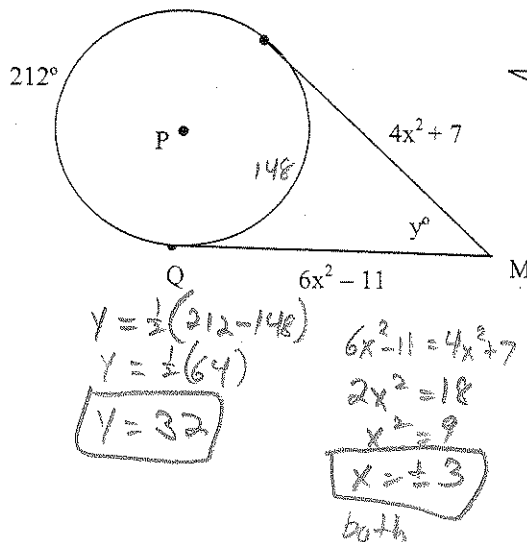
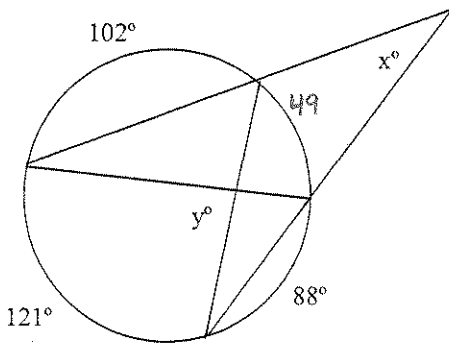
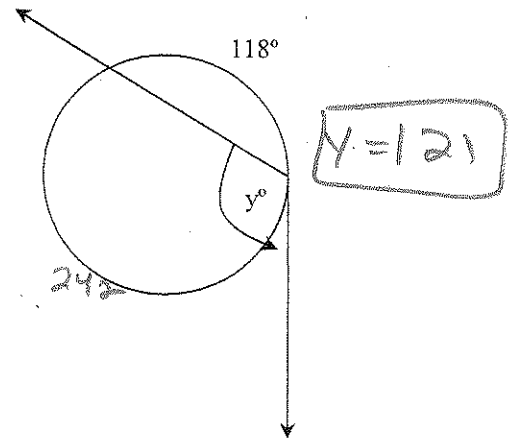
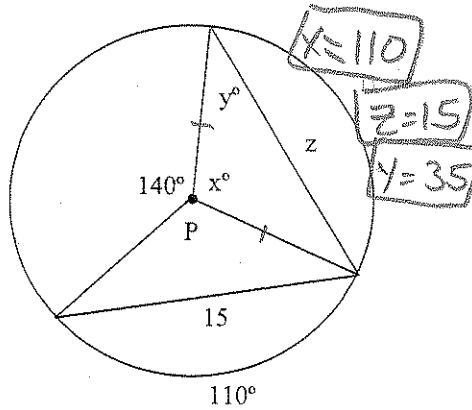
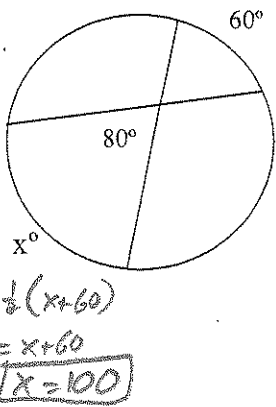
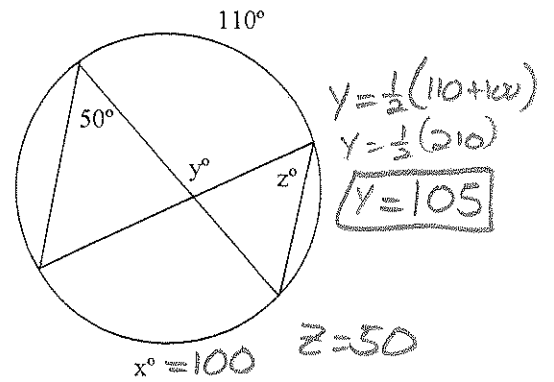
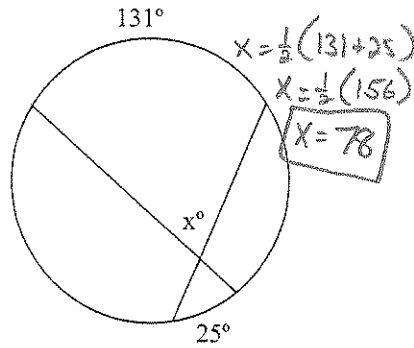
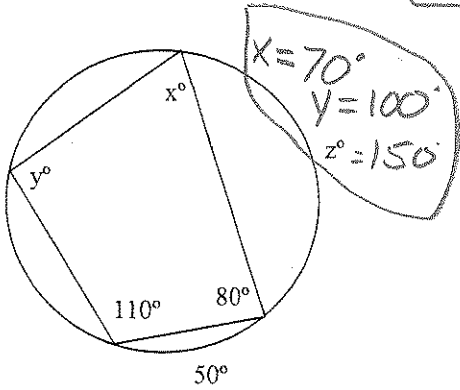
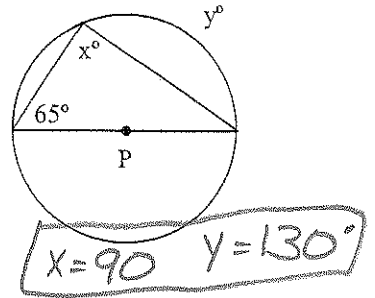
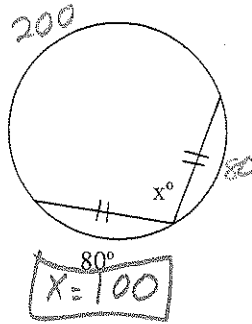
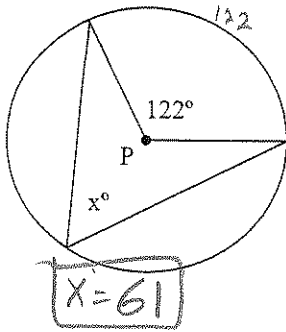
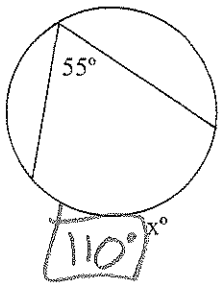
$$m\widehat{ADK} = 212^\circ$$

$$m\widehat{ADB} = 302^\circ$$

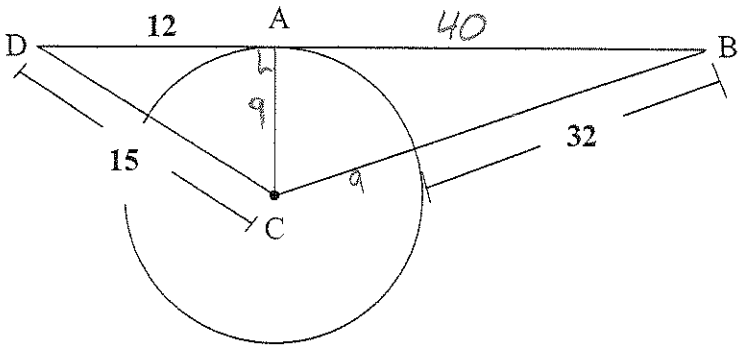
$$m\angle AQB = 148^\circ$$

$$m\widehat{BAD} = 180^\circ$$

4. Find  $x$ ,  $y$ , and/or  $z$  in each figure.  $P$  is the center if present.



5. In the diagram below,  $\overline{DB}$  is tangent to Circle C.



a.  $\overline{CA} \perp \overline{DB}$  at point A. (mark this in diagram)

b. Find the length of the radius.

$$15^2 - 12^2 = r^2$$

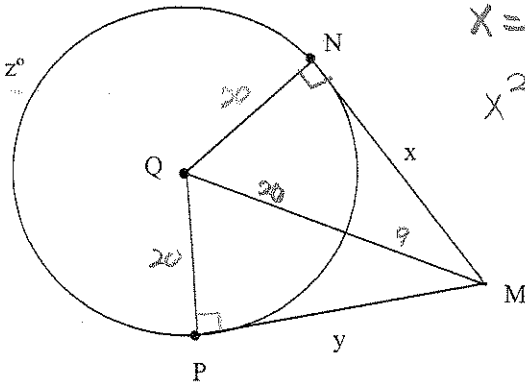
$$\boxed{r=9}$$

c. Find the length of  $\overline{AB}$ .

$$41^2 - 9^2 = AB^2$$

$$\boxed{AB=40}$$

6.  $\overline{MN}$  and  $\overline{MP}$  are tangent to circle Q with radius 20.  $QM = 29$ . Find x, y, and z.



$$x=y$$

$$x^2 + 20^2 = 29^2$$

$$x = \sqrt{29^2 - 20^2}$$

$$\boxed{x=y=21}$$

$$\sin \angle PMQ = \frac{20}{29}$$

$$m\angle PMQ = \sin^{-1}\left(\frac{20}{29}\right)$$

$$m\angle PMQ = 43.6^\circ$$

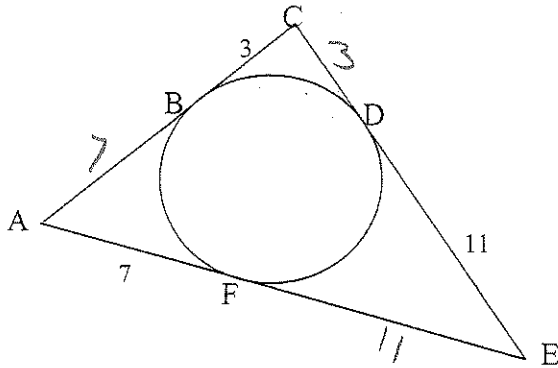
$$m\angle PMN = 87.2^\circ$$

$$87.2 = \frac{1}{2}(z - (360 - z))$$

$$174.4 = 2z - 360$$

$$\boxed{z=267.2}$$

7. The sides of the triangle below are tangent to the circle. Find the perimeter of the triangle.



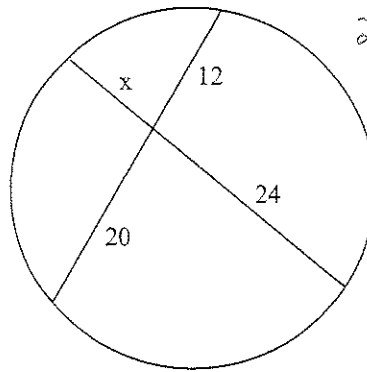
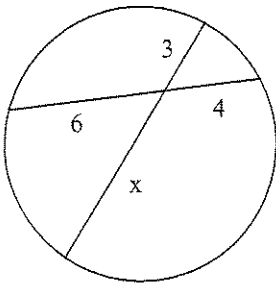
$$P = 10 + 14 + 18$$

$$\boxed{P=42}$$

8. Find  $x$ , the length of missing segments.

$$3x = 24$$

$$x = 8$$



$$24x = 12 \cdot 20$$

$$24x = 240$$

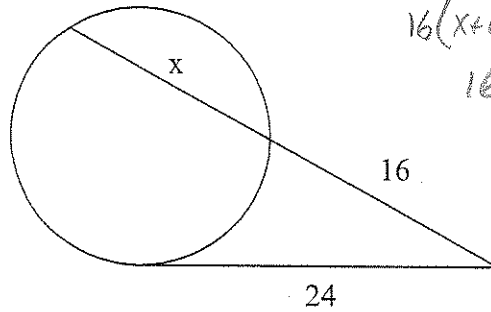
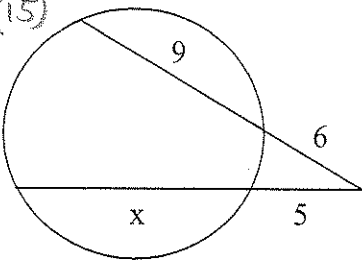
$$x = 10$$

$$5(x+5) = 6(15)$$

$$5x+25 = 90$$

$$5x = 65$$

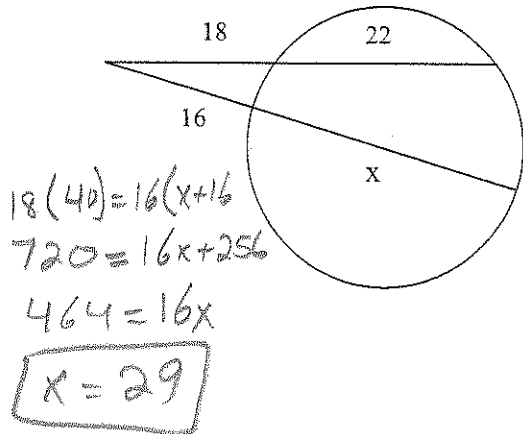
$$x = 13$$



$$16(x+16) = 24^2$$

$$16x + 256 = 576$$

$$x = 20$$

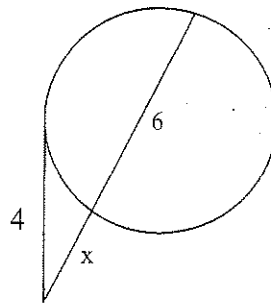


$$18(40) = 16(x+16)$$

$$720 = 16x + 256$$

$$464 = 16x$$

$$x = 29$$



$$x(x+6) = 4^2$$

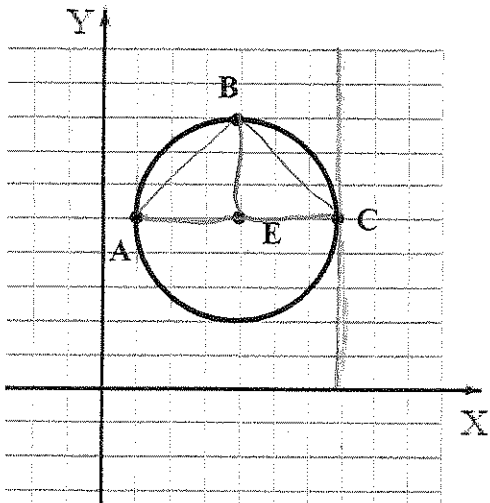
$$x^2 + 6x = 16$$

$$x^2 + 6x - 16 = 0$$

$$(x+8)(x-2) = 0$$

$$x = -8 \quad x = 2$$

9. Study Circle E in the coordinate plane below.



a. Give the coordinates of the center of the circle  $(4, 5)$

b. Give the length of the radius Circle E. (Draw in radii  $\overline{AE}$ ,  $\overline{BE}$ , and  $\overline{CE}$ .)

$$3$$

c. Find the length of chord  $\overline{AB}$  and chord  $\overline{CB}$ . (Draw them.)

$$AB = 3\sqrt{2}$$

$$CB = 3\sqrt{2}$$

d. Give the degree measure of arcs  $\widehat{AB}$  and  $\widehat{CB}$

$$m\widehat{AB} = m\widehat{CB} = 90^\circ$$

e. Sketch a tangent that passes through C.

10. Write the standard equation of the circle.

a. Center (0, 0), radius 9

$$x^2 + y^2 = 81$$

b. Center (1, 3), radius 4

$$(x-1)^2 + (y-3)^2 = 16$$

c. Center (-3, 0), radius 5

$$(x+3)^2 + y^2 = 25$$

d. Center (0, 0), point on circle (3, -4)  $r=5$

$$x^2 + y^2 = 25$$

e. Center (-1, 4), diameter 20

$$(x+1)^2 + (y-4)^2 = 100$$

$r=10$

f. Center (2, 3), diameter 30  $r=15$

$$(x-2)^2 + (y-3)^2 = 225$$

11. Determine the diameter of the circle with the given equation.

a.  $x^2 + y^2 = 100$

$$d = 20$$

b.  $(x-12)^2 + (y+5)^2 = 64$

$$d = 16$$

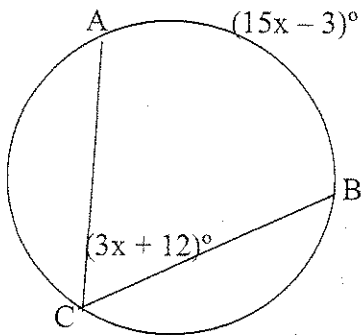
c.  $(x-2)^2 + (y-9)^2 = 4$

$$d = 4$$

d.  $(x+16)^2 + (y+15)^2 = 81$

$$d = 18$$

12. Find the value of x.



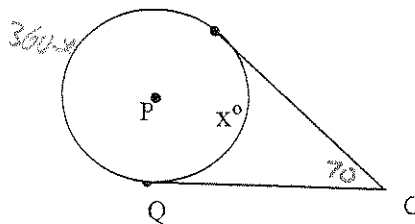
$$3x + 12 = \frac{1}{2}(15x - 3)$$

$$6x + 24 = 15x - 3$$

$$27 = 9x$$

$$3 = x$$

13. If  $m\angle C = 70$ , find x.



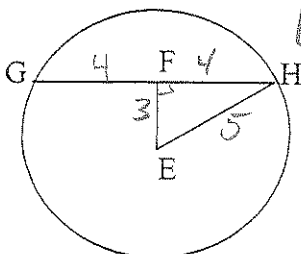
$$70 = \frac{1}{2}(360 - x - x)$$

$$140 = 360 - 2x$$

$$2x = 220$$

$$x = 110$$

14. The radius is 5.  $EF = 3$ . Find GH.



$$GH = 8$$

iffy?

