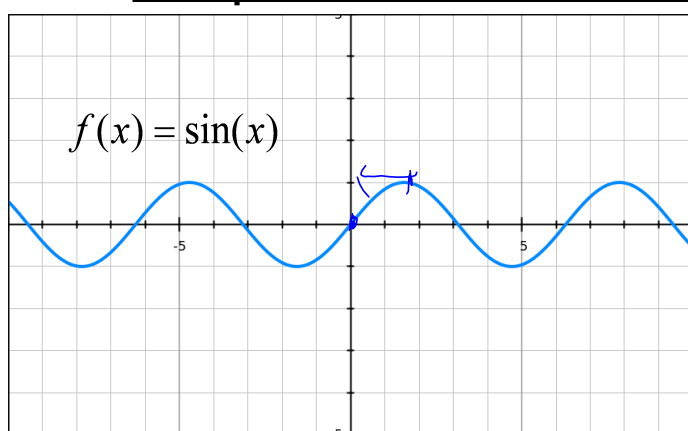


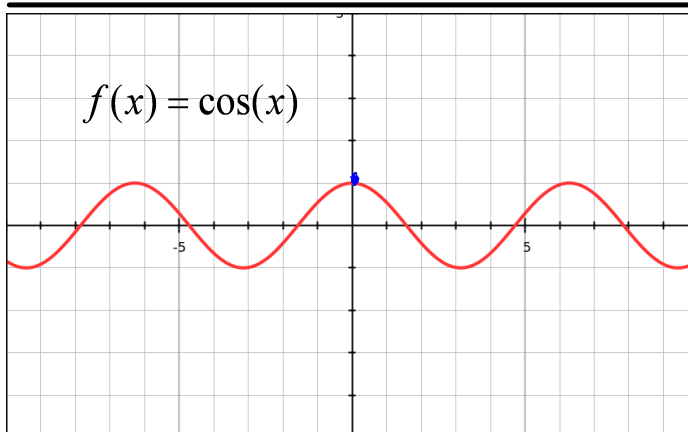
## Sec 4.5

### Graphs of the Sine and Cosine Functions



Domain: All Real numbers  
(radians or degrees)

Range:  $-1 \leq y \leq 1$

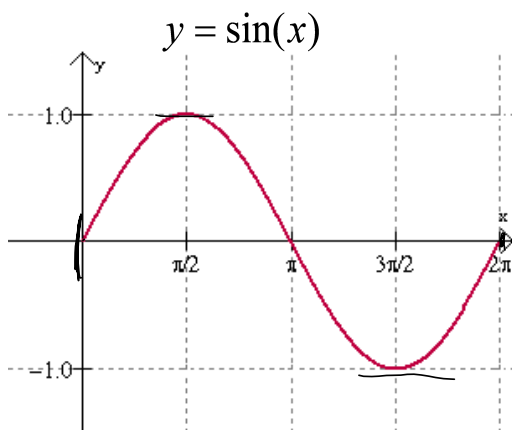


Domain: All Real numbers  
(radians or degrees)

Range:  $-1 \leq y \leq 1$

### Characteristics of Trig Functions

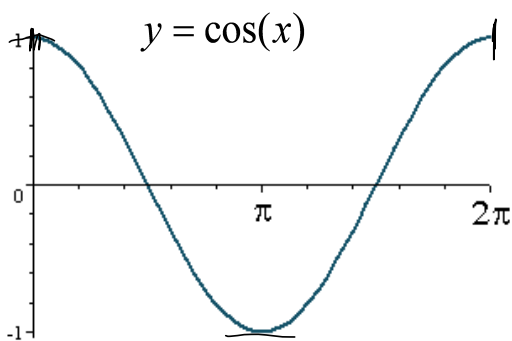
- all trig functions repeat themselves, the horizontal distance it takes for the graph to repeat itself is called the period.
- the sine and cosine functions have an amplitude. It is defined as half the distance between the maximum and minimum values.



For the basic sine function

period =  $2\pi$

amplitude = 1



For the basic cosine function

period =  $2\pi$

amplitude = 1

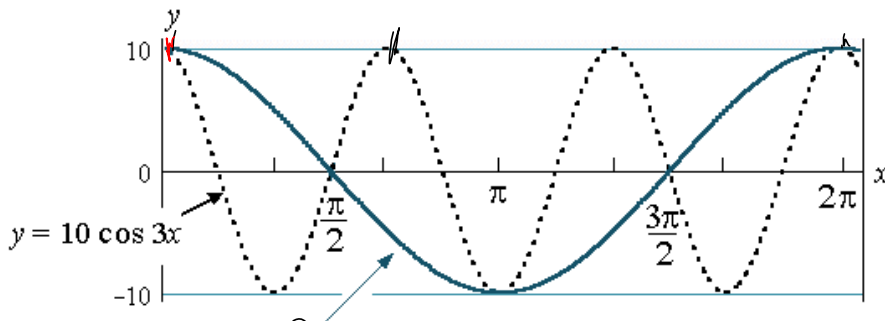
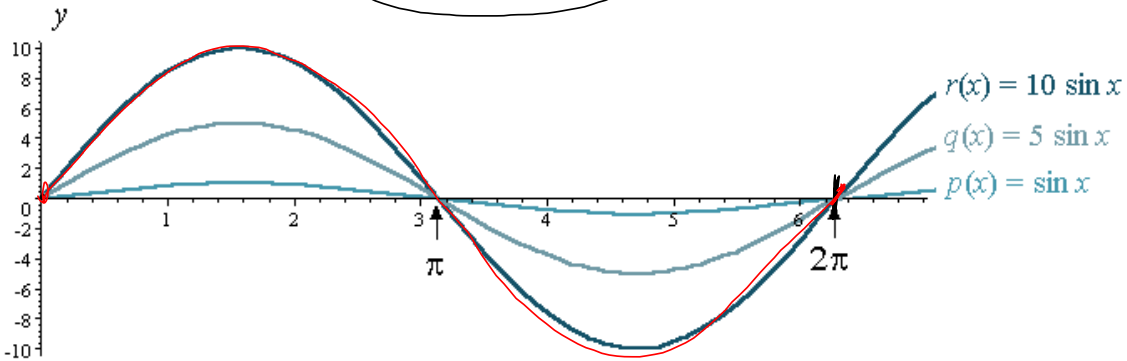
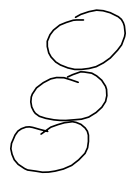
The sine & cosine graphs can be changed to any size wave by changing some things in the equation. Right now we are going to concentrate on amplitude and period.

$$y = a \sin(bx) \qquad y = a \cos(bx)$$

$|a| = \text{amplitude}$

$$\frac{2\pi}{b} = \text{period}$$

$-4 \sin x$



$y = 10 \cos x$   
 $\frac{2\pi}{1} = 2\pi$

$\frac{2\pi}{3}$

go to applet page

Example Identify the amplitude and period from the equations

$$y = -4 \cos(4x)$$

$$\text{amp} : 4$$

$$\text{Per} : \frac{2\pi}{4} = \frac{\pi}{2}$$

$$y = a \cdot \cos(bx)$$

$$a = -4$$

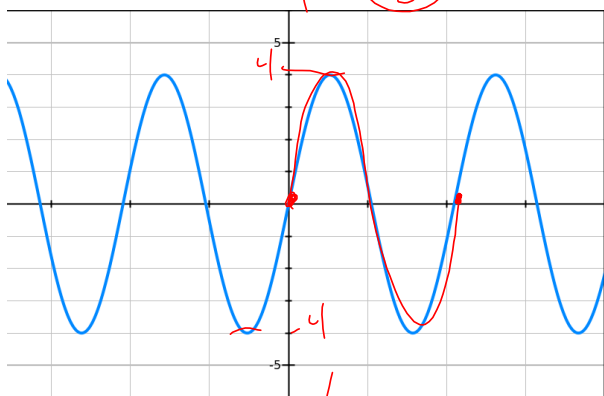
$$b = 4$$

$$y = \frac{1}{2} \sin\left(\frac{2\pi x}{3}\right)$$

$$b = \frac{2\pi}{3}$$

$$\text{amp} : \frac{1}{2}$$

$$\text{Per} : \frac{2\pi}{\frac{2\pi}{3}} = 2\pi \cdot \frac{3}{2\pi}$$



$$\text{amp} : 4$$

$$\text{Per} : 2.1$$

⊖

$$\frac{2\pi}{b} = 2.1$$

3

$$y = \sin\left(\frac{2\pi}{2.1} x\right)$$

Day 2 Start

The amplitude and period are stretches of the basic sine & cosine functions. A phase shift is a horizontal shift of a trig function.

$$y = d + a \sin(bx - c) \qquad y = d + a \cos(bx - c)$$

*Left/right*

*bx - c*

- these variables do the same thing to the sine and cosine graphs

$d$  = vertical shift  $\longrightarrow$  positive  $\Rightarrow$  shift up      negative  $\Rightarrow$  shift down

$\frac{c}{b}$  = phase shift  $\longrightarrow$  you need to compare the equation to the generic above, when it is  $bx - c$ , shift right. when it is  $bx + c$ , shift left

$|a|$  = amplitude

$$\frac{2\pi}{b} = \text{Period}$$

the left and right endpoints of a one-cycle interval can be found by solving the two equations  $bx - c = 0$  and  $bx - c = 2\pi$

Example

Identify the amplitude, period, phase shift and vertical shift.

$$y = \frac{1}{2} \sin\left(x - \frac{\pi}{3}\right)$$

$$Y = d + a \sin(bx - c)$$

$$a = \frac{1}{2}$$

$$b = 1$$

$$c = \frac{\pi}{3}$$

$$d = 0$$

$$\text{amp} : \frac{1}{2}$$

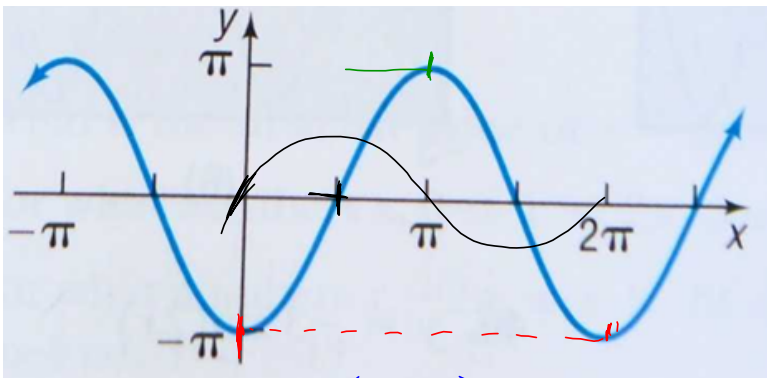
$$\frac{2\pi}{b} \text{ Per} : 2\pi$$

$$\frac{c}{b} \text{ P.S.} : \frac{\pi}{3}$$

$$\text{V.S.} : \bigcirc$$

(right)

Write the equation that would produce this graph.



$$y = d + a \cos(bx - c)$$

$$|a| = \text{amp} = \pi$$

$$b \rightarrow \frac{2\pi}{1} = \text{Period} = 2\pi \rightarrow b = 1$$

$$c \rightarrow \frac{c}{b} = \text{Phase shift} \rightarrow \pi = c$$

$$d = 0$$

Sine

$$c \rightarrow \frac{c}{b} = \frac{\pi}{2}$$

$$c = \frac{\pi}{2}$$

$$y = \pi \sin\left(x - \frac{\pi}{2}\right)$$

