

4.1 to 4.4 Worksheet

List one positive and one negative coterminal angle for:

1) 187 degrees 547° degrees -173° degrees

2)  $\frac{5\pi}{3}$  radians  $-\frac{\pi}{3}$  radians  $\frac{11\pi}{3}$  radians

3) Find the radius of a circle with a central angle of  $60^\circ$  that intercepts an arc of 12 cm

$S = r\theta$   
 $\frac{3}{\pi} \cdot 12 = r \cdot \frac{\pi}{3}$

$\frac{\pi}{3}$  rad.

$\frac{36}{\pi} = r$   
 $\approx 11.459$  cm

4) Find the arc length when a circle of radius 12 m has a central angle of  $5\pi$

$S = r\theta$   
 $= 12 \cdot 5\pi$   
 $S = 60\pi$  m

5) A saw blade has a radius of 6 inches (1/2 foot). It rotates at 1000 revolutions per minute. What is the linear speed of the teeth on the edge of the blade (in ft/min)?

Speed =  $\frac{S}{t} = \frac{r\theta}{t} = \frac{\frac{1}{2}(2\pi \cdot 1000)}{1 \text{ min}} = 1000\pi \frac{\text{ft}}{\text{min}} \approx 3141.5 \frac{\text{ft}}{\text{min}}$

6) Find all values that satisfy the equation for  $\theta$  from  $0 \leq \theta \leq 2\pi$

a.  $\sin\theta = \frac{-\sqrt{3}}{2}$   $\theta = \frac{4\pi}{3}; \frac{5\pi}{3}$

b.  $\cos\theta = \frac{\sqrt{2}}{2}$   $\theta = \frac{\pi}{4}; \frac{7\pi}{4}$

7) Find the values of the following:

a.  $\sin 45^\circ = \frac{\sqrt{2}}{2}$

b.  $\tan 30^\circ = \frac{1}{\sqrt{3}} = \frac{1}{2} \cdot \frac{2}{\sqrt{3}} = \frac{1}{\sqrt{3}}$  or  $\frac{\sqrt{3}}{3}$

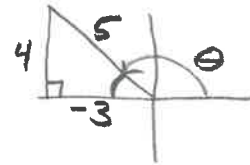
c.  $\cos \frac{2\pi}{3} = -\frac{1}{2}$

d.  $\cot 2\pi = \frac{1}{0} \Rightarrow$  Undefined

8) Find the values of the  $\sin\theta$  and  $\cos\theta$  given that  $\tan\theta = \frac{-4}{3}$  and  $\theta$  is in Q II

$\sin\theta = \frac{4}{5}$

$\cos\theta = \frac{-3}{5}$



9) Find the exact (no decimals) values of the 6 trig functions of the angle  $\theta$  in a right triangle if side  $a = 9$  and the hypotenuse = 14.

$\sin\theta = \frac{\sqrt{115}}{14}$

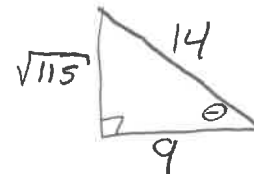
$\csc\theta = \frac{14}{\sqrt{115}}$

$\cos\theta = \frac{9}{14}$

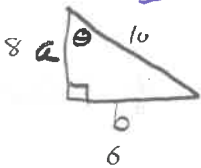
$\sec\theta = \frac{14}{9}$

$\tan\theta = \frac{\sqrt{115}}{9}$

$\cot\theta = \frac{9}{\sqrt{115}}$



10) Solve for the missing side lengths in a right triangle (round to 4 decimal places) Given side  $a = 8$ , and angle  $A$  ~~is~~ exact values of all 6 trig functions



side  $b = 6$

$\sin\theta = \frac{6}{10}$      $\csc\theta = \frac{10}{6}$

$\cos\theta = \frac{8}{10}$      $\sec\theta = \frac{10}{8}$

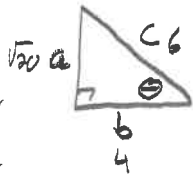
$\tan\theta = \frac{6}{8}$      $\cot\theta = \frac{8}{6}$

Side  $b$  \_\_\_\_\_

Side  $c$  \_\_\_\_\_

6 trig Functions (exact values)

11) Solve for the ~~missing angles~~ (in degrees) of right triangle ABC if side  $b = 4$  and side  $c = 6$



$\sin\theta = \frac{\sqrt{20}}{6}$      $\csc\theta = \frac{6}{\sqrt{20}}$

$\cos\theta = \frac{4}{6}$      $\sec\theta = \frac{6}{4}$

$\tan\theta = \frac{\sqrt{20}}{4}$      $\cot\theta = \frac{4}{\sqrt{20}}$

Angle  $A$  = \_\_\_\_\_

Angle  $B$  = \_\_\_\_\_

$a^2 + 4^2 = 6^2$   
 $a^2 = \frac{36}{16}$   
 $a = \sqrt{20}$

12) The point  $(-24, 7)$  is on the terminal side of an angle in standard position. Find the exact values of sine, cosine and tangent of the angle  $\theta$ .

$\sin\theta = \frac{7}{25}$

$\cos\theta = \frac{-24}{25}$

$\tan\theta = \frac{7}{-24}$

